Question 1 Don't forget cylindrical and spherical coordinates and quadric surfaces.

Question 2 Let $f(x,y) = x \sin(y/x)$. Find the partial derivatives: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial^2 f}{\partial y \partial x}$

Question 3 Find and sketch the domain of the function $f(x,y) = \frac{5}{\sqrt{10 - 2y^2 - x^2}}$.

Question 4 Evaluate the following limit:

$$\lim_{(x,y)\to(1,2)}\frac{\sqrt{x+y}-\sqrt{3}}{x+y-3}$$

Question 5 Show that the following limit does not exist as $(x, y) \to (0, 0)$ by considering different paths of approach.

$$\lim_{(x,y)\to(0,0)} \frac{x^2y+y^2}{x^4+y^2}$$

Question 6 Let w = f(u, v) be a function whose derivatives of all orders exist. Suppose that $\frac{\partial^2 f}{\partial u^2}(0,2) = 0$, $\frac{\partial^2 f}{\partial u^2}(3,0) = -3$, $\frac{\partial^2 f}{\partial u \partial v}(0,2) = 2$, $\frac{\partial^2 f}{\partial u \partial v}(3,0) = 3$, $\frac{\partial^2 f}{\partial v^2}(0,2) = 1$, $\frac{\partial^2 f}{\partial v^2}(3,0) = -1$. If $u = y + e^{2x}$ and v = xy, what is the value of $\frac{\partial^2 w}{\partial y^2}$ evaluated at the point (x,y) = (0,2).

Question 7 Find the direction in which $f(x, y) = x^2 + \cos xy$ increases most rapidly at the point $(1, \pi/2)$. What is the rate at which f changes in that direction? What is the euqation of the tangent plane at the point $(1, \pi/2)$?

Question 8 Find the critical points of the function

$$f(x,y) = x^4 - x^2y + \frac{3}{4}y^2 - 2y + 5$$

and determine all relative maximum, relative minimum, and saddle points.